Role of dressed-state interference in electromagnetically induced transparency

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Electromagnetically induced transparency (EIT) in three-level systems uses a strong control laser on one transition to modify the absorption of a weak probe laser on a second transition. The control laser creates dressed states whose decay pathways show interference. We study the role of dressed-state interference in causing EIT in the three types of three-level systems—lambda (Λ), ladder (Ξ), and vee (V). In order to get realistic values for the linewidths of the energy levels involved, we consider appropriate hyperfine levels of $^{87}$Rb. For such realistic systems, we find that dressed-state interference causes probe absorption—given by the imaginary part of the susceptibility—to go to zero in a Λ system, but plays a negligible role in Ξ and V systems.

1. Introduction

Electromagnetically induced transparency (EIT) [1,2] is a phenomenon in which a strong control laser is used to modify the properties of a medium for a weak probe laser. The phenomenon uses the fact that most optical media are composed of multilevel atoms, so that the control and probe beams can act on different transitions. Applications of EIT include slowing of light [3] (for use in quantum-information processing), lasing without inversion [4], enhanced nonlinear optics [5,6], high-resolution spectroscopy [7–9], and getting subnatural linewidth for tight locking of lasers to optical transitions [10,11].

EIT occurs due to two effects caused by the strong control laser—(i) AC Stark shift of the atomic levels leading to the creation of new eigenstates of the coupled atom plus photon system called dressed states [see Refs. [12,13]; but with the interaction Hamiltonian included as described in Ref. [2]], and (ii) the interference between the decay pathways to or from these dressed states. The dressed-state approach is better because it is valid at all intensities (page 98 of Ref. [14]), whereas the one used in Ref. [15] is valid only at high intensities. The degree of interference depends on the linewidth of the dressed states, and the role of this interference in EIT is not well studied in all three-level systems.

In this work, we study in detail the dressed-state linewidth and interference in the three canonical types of three-level atoms—lambda (Λ), ladder (Ξ), and vee (V). For specificity, we choose hyperfine energy levels of $^{87}$Rb. This allows us to use realistic values of the decay rates, which is important since it influences the degree of interference in Ξ and V systems that involve multiple excited states. We find that the dressed-state linewidth steadily increases over these three systems. In addition, interference causes probe absorption to vanish identically at line center in Λ systems because of the formation of a dark state. As expected, the effect of interference decreases with increasing Rabi frequency of the control laser, since it causes increasing separation of the dressed states.

2. Dressed-state location and linewidth

We define the three atomic levels as $|1\rangle$, $|2\rangle$, and $|3\rangle$. The probe laser drives the $|1\rangle \leftrightarrow |2\rangle$ transition with Rabi frequency $\Omega_p$ and detuning $\Delta_p$. The strong control laser drives the $|2\rangle \leftrightarrow |3\rangle$ transition with Rabi frequency $\Omega_c$ and detuning $\Delta_c$. Both these transitions are electric dipole (E1) allowed, and the levels involved have opposite parity. Therefore, the $|1\rangle \leftrightarrow |3\rangle$ transition involves levels of the same parity and is E1 forbidden. The level $|i\rangle$ is assumed to have a spontaneous decay rate of $\Gamma_i$. Since ground levels have zero decay rate, depending on the particular three-level system, one or more of the $\Gamma_i$’s will be zero.

The 3 three-level systems are shown in Fig. 1. Theoretical analysis for each system is done using a standard density matrix analysis of the three levels involved. Time evolution of the elements is given by the general equation:

$$\frac{d\rho}{dt} = -\frac{i}{\hbar} [H, \rho] - \frac{1}{2} \{\Gamma, \rho\}$$

(1)
where $H$ is the Hamiltonian governing the atom–photon interaction, and $\Gamma$ is the relaxation rate. The coherence induced on the probe transition is given by the element $\rho_{12}$. Therefore, probe absorption is proportional to its imaginary part, while probe dispersion is proportional to its real part. In the following, we will operate in the weak-probe limit, i.e. $\Omega_p \ll \Omega_c$.

The dressed states created by the control laser are shifted in energy by the AC stark shift. Therefore they are located at values of $\Delta_p$ given by:

$$\Delta_{\pm} = \frac{\Delta_c}{2} \pm \frac{1}{2} \sqrt{\Delta_c^2 + \Omega_c^2}$$

If we consider the special case of $\Delta_c = 0$, i.e. control laser on resonance, then probe absorption splits into the expected Autler–Townes doublet with peaks located at $\pm \Omega_c/2$. Since the control laser couples levels $|2\rangle$ and $|3\rangle$, the linewidth of each dressed state is given by:

$$\Gamma_{ds} = \frac{\Gamma_2 + \Gamma_3}{2}$$

The probe laser couples levels $|1\rangle$ and $|2\rangle$, hence the linewidth of each sub-peak in the probe absorption spectrum is:

$$\Gamma_p = \Gamma_1 + \frac{\Gamma_2 + \Gamma_3}{2}$$

In the following, the above expression will be used to determine the linewidth of the Autler–Townes doublet in the 3 three-level systems.

### 3. EIT in a lambda system

We first consider the $\Lambda$ system shown in Fig. 1(a). The energy levels of $^{87}$Rb used to form this system are shown in the table below.

<table>
<thead>
<tr>
<th>Level</th>
<th>$^{87}$Rb hyperfine level</th>
<th>$\Gamma/2\pi$ (MHz)</th>
<th>Wavelength (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$</td>
<td>1\rangle$</td>
<td>$S_1/2$, $F = 1$</td>
<td>0</td>
</tr>
<tr>
<td>$</td>
<td>2\rangle$</td>
<td>$S_1/2$, $F = 2$</td>
<td>6.1</td>
</tr>
<tr>
<td>$</td>
<td>3\rangle$</td>
<td>$S_1/2$, $F = 2$</td>
<td>0</td>
</tr>
</tbody>
</table>

As seen, $|2\rangle$ is an excited state, and $|1\rangle$ and $|3\rangle$ are ground levels. Therefore, $\Gamma_1 = \Gamma_3 = 0$ and $\Gamma_2$ is non-zero.

In order to ensure a steady state approach ($\dot{\rho} = 0$) is valid, we have studied the transient behavior of the density-matrix elements of this system. Probe absorption, which is given by $\text{Im}(\rho_{12} \Gamma_2/\Omega_p)$, is plotted in Fig. 2 for 5 values of $\Omega_c$ (negative absorption means gain). It is clear that transient oscillations die down after a few lifetimes $\Gamma_2$ of the excited state. Thus, the system will reach steady state within the time frame used in the experiment, and the density-matrix equations can be solved under this condition. Such an analysis yields [16]:

$$\rho_{12} = \frac{i \Omega_p}{\Omega_c} \frac{\Gamma_2}{2}$$

From Eq. (4), we get the linewidth of the Autler–Townes doublet as

$$\Gamma_{AT} = \frac{\Gamma_2}{2}$$

Thus, probe absorption splits into two peaks, each with a linewidth of half the original linewidth.

The above description ignores any interference between the decay pathways to the two dressed states. If we take that into account, there is destructive interference at line center and probe absorption goes identically to zero. For low values of control Rabi frequency $\Omega_c \ll \Gamma_2$, this interference can make the EIT dip extremely narrow. Such dressed-state interference in a $\Lambda$ system has been observed before using the $D_1$ line of Rb [17]. The effect of this interference is seen clearly in our calculations shown in Fig. 3. The solid lines represent the complete density-matrix calculation, while the dashed lines are what the spectrum would look like with just the two dressed states of linewidth $\Gamma_2/2$ and no interference. A quantitative measure of what is shown in the figure is seen in the table below (at line center, $\Delta_p = 0$). The last column, which gives the difference between having and not having interference, shows that the effect of interference decreases as the control Rabi frequency is increased.
Here, the two levels coupled by the control are both excited, therefore $\Gamma_2^\prime$ and $\Gamma_\gamma^\prime$ are non-zero and $\Gamma_1^\prime = 0$.

As before, we study the transient behavior to verify that a steady state solution is valid. Probe absorption spectra, given by $\text{Im}(\rho_{12}\Gamma_2^\prime/\Omega_\rho^\prime)$ and plotted in Fig. 4, show that all transient oscillations die down after a few lifetimes $\Gamma_2^\prime$ of the excited state. Thus, the density-matrix analysis can be done in steady state, which yields a solution of [9]:

$$\rho_{12} = \frac{i\Omega_p/2}{\left(\Gamma_2^\prime - i\Delta_p\right) + i\Omega_c^2/4 - i(\Delta_p + \Delta_\gamma)}$$  \hspace{1cm} (7)

EIT spectra are shown in Fig. 5. Again taking the special case of control on resonance $\Delta_\gamma = 0$, we see from the figure that each spectrum splits into two (Autler-Townes doublet) with a transparency dip at line center. From Eq. (4), the linewidth of each sub-peak is:

$$\Gamma_{AT} = \frac{\Gamma_2^\prime + \Gamma_\gamma^\prime}{2}$$  \hspace{1cm} (8)

But in this case the absorption at line center does not go to zero, because no stable dark state is formed. In addition, interference causes the transparency dip to increase from that of the
5. EIT in a veec system

We finally consider the V system shown in Fig. 1(c). The energy levels of $^{87}$Rb used to form this system are shown in the table below.

<table>
<thead>
<tr>
<th>Level</th>
<th>$^{87}$Rb hyperfine level</th>
<th>$\Gamma / 2\pi$ (MHz)</th>
<th>Wavelength (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>5P_{1/2}, F = 1</td>
<td>6.1</td>
<td>$\lambda_p = 780.24$</td>
</tr>
<tr>
<td>2</td>
<td>5S_{1/2}, F = 1</td>
<td>0</td>
<td>$\lambda_c = 780.24$</td>
</tr>
<tr>
<td>3</td>
<td>5P_{3/2}, F = 2</td>
<td>6.1</td>
<td></td>
</tr>
</tbody>
</table>

Here, the common level is a ground level, and both the control and probe lasers couple to excited levels. Therefore, $\Gamma_1$ and $\Gamma_3$ are non-zero and $\Gamma_2 = 0$. In this case, probe absorption is given by $\text{Im}[\rho_{21}/\Omega_p]$.

Transient spectra, shown in Fig. 6, show that the system reaches steady state after a few lifetimes $\Gamma_1$ of the excited state. Hence this system is also analyzed in steady state, which yields a solution of [19]:

$$
\rho_{21} = \frac{i\Omega_p}{2(\Gamma_1^2 + 4\Delta^2 + |\Omega_c|^2)} \left[ \left( \Gamma_1^2/2 + i\Delta_p \right) \frac{\Gamma_3}{\Gamma_1 + \Gamma_3} \right] + \frac{|\Omega_c|^2/4}{\Gamma_1 + \Gamma_3} \left( \frac{\Gamma_3}{\Gamma_1 + \Gamma_3} \right) + i(\Delta_c - \Delta_p) \right]
$$

Thus, EIT in a V system is almost exclusively dependent on the AC Stark shift with negligible role for dressed-state interference.

6. Conclusion

In summary, we have studied the linewidth of the dressed states and the role of interference in the three types of three-level systems. All the three show an Autler–Townes doublet structure
in the probe-absorption spectrum. This results in a transparency window at line center, which is the main cause for EIT in these systems. However, dressed-state interference plays an equally important role in the phenomenon of EIT in a lambda system. This causes the EIT dip to zero identically to zero at line center—this can result in an extremely narrow transparency window when the control power is very small. By contrast, dressed-state interference plays a negligible role in ladder and vee systems.

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